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Event reconstruction in IceCube based on direct event re-simulation

THE ICECUBE COLLABORATION[1]

[1]*See special section in these proceedings*

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Abstract: We present a new method of event reconstruction in IceCube that searches through an extensive set of re-simulated events to find the best match to data. Several search methods, including the stochastic approximation and localized random search, were tried. We demonstrate the capability of the new method to reconstruct cascade-like as well as track-like events. While significantly slower than the parametrized probability density function (PDF) -based reconstructions, the new method is able to take into account all of the nuances present in the simulation that are sometimes omitted from the PDF-based description of data.

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1 Introduction

IceCube is a cubic-kilometer neutrino detector installed in the ice at the geographic South Pole [1] between depths of 1450 m and 2450 m. Detector construction started in 2005 and finished in 2010. Event reconstruction relies on the optical detection of Cherenkov radiation emitted by secondary particles produced in neutrino interactions in the surrounding ice or the nearby bedrock.

The development of the method described in this paper was prompted by our recognition that ice surrounding the detector does not have the azimuthal symmetry previously ascribed to it (see [2], [3]) and still used in our probability density function (PDF) -based event reconstructions. While it is relatively easy to add a description of almost any conceivable detail to the detector simulation, adding even one new dimension to the existing photon propagation probability tables is prohibitive. This is due to the large computing time necessary to create the PDF tables, and also due to the excessive storage requirements of and the speed of access to the stored tables (the latter becomes slow if the tables cannot be fitted into the active computer memory).

In section 2 we discuss reconstruction of cascades, i.e., relatively short particle showers, which happen when neutrinos interact via the neutral current process, or when ν_e, $\bar{\nu}_e$ and ν_τ, $\bar{\nu}_\tau$ interact via the charged current process. In these cases all visible particles produced in the interaction are short-lived, either decaying or losing energy very quickly, producing an initial light pattern that can often be approximated as emanating from a point, when compared to the large scale of the IceCube detector.

In contrast, the charged current interactions of ν_μ, $\bar{\nu}_\mu$ create a muon (in addition to the initial cascade), which can propagate a great distance away from the interaction point, leaving behind a characteristic "track"-like pattern of light. We call these events "tracks" and discuss the application of our method to the track-like events in section 3.

2 Cascade reconstruction

We start by describing the cascade reconstruction, the purpose of which is to ascertain the parameters of the cascade-like event observed in data: energy (E), time and position (t_0, x, y, z), and direction (θ, ϕ). The algorithm works by simulating many cascades with various sets of parameters and choosing the one (or a few) that look most like data.

We compare the time-binned photo-electron charges registered by optical sensors between data and simulation with a likelihood function described in [4], which takes into account statistical fluctuations in both data and simulation. A systematic disagreement between data and simulation is modeled with a log-normal distribution (describing the "model error" of the ice model, as explained in [2] and reduced to 20% in [3]).

We obtained the best performance with the "localized random search"-based optimization method. The reconstruction is started from a first guess with the coordinates of the center of gravity of hits in the detector, a random direction, the energy of $E = 10^5$ GeV, and the start time t_0 coincident with the time of the first hit in the event. We also specify the widths of the proposal distributions for space coordinates (Δr=10 m) and angular coordinates ($\Delta\Psi$=30 degrees). The proposal distributions are the 3D Gaussian and 2D Gaussian on a sphere (von-Mieses-Fisher distribution).

At each iteration 25 possible sets of space and angular coordinates (x, y, z, θ, ϕ) are sampled from the proposal distribution around the best cascade from the previous iteration (or the initial guess, if this is the first iteration). For each such set the photon simulation of [6] is run with the best values of E and t_0 from the previous iteration, producing Monte-Carlo hits. Then the best values of energy E and start time t_0 that maximize the likelihood function are found. This is done by scaling the simulation (varying n_s of [4]) and shifting it in time. Finally, each set is re-simulated with the optimized values of E and t_0. The final likelihood values for all 25 sets are computed and the event with the best value is selected. This best value and corresponding cascade parameters are saved and used as a starting point for the next iteration.

This process is repeated 400 times. Every 40 iterations the proposal distribution width parameters Δr and $\Delta\Psi$ are updated to the RMS values of space and angular coordinates calculated from the best 20 of the previous 40 iterations. Finally, the solution is calculated by averaging the best 160 iteration results. Their spread can be used as a rough measure of statistical uncertainties, and is immediately available as it is calculated during reconstruction (unlike the more rigorous procedure described in section 4). The specific numbers listed above (25 sets per iteration, 400 iterations, initial parameters of the proposal distribution) resulted in a robust, yet relatively fast reconstruction.

In addition to the "localized random search" method described above we have tried two more approaches, which yielded somewhat less robust performance. The first of these is the simultaneous perturbation stochastic approximation [5] and its variations, which is a derivative-based maximization search method, where the derivative is calculated "stochastically" from consecutive iterations, and the step size is reduced in a controlled manner. The second method is the Markov chain Monte-Carlo with each proposed step either taken or rejected based on whether the calculated value of the likelihood at the new coordinates is better or worse than that at the current point. Since the likelihood value at given coordinates is calculated from a simulation performed anew for each new evaluation, it is a "stochastic" quantity, forming a distribution, rather than assuming a single value. So, it is possible to jump from a point with parameters providing a (on average) better description of data to a point with parameters providing a (on average) worse description of the data. Although the iterations of the method do, in fact, form a Markov chain, this Markov chain is not expected to be reversible, with no obvious probabilistic interpretation of the resulting sequence of iterations.

3 Track reconstruction

The algorithm described in the previous section also works for track reconstruction with the following modification, which consists of one or more "passes". We start by describing the first pass. For each proposed set of space and angular coordinates defining a track (x, y, z, θ, ϕ), small cascades of equal energy are simulated every 7.5 meters along the part of the track that is inside the detector with a fixed combined energy of 10^6 GeV. Each such cascade (numbered with index j) produces a pattern of hits in the detector, creating a column in a matrix A_{ij}, where i represents a time bin in a DOM (A_{ij} being the photo-electron charge in that bin left by the cascade j).

We now have an unfolding problem similar to that discussed in [7], where the energy of each cascade j needs to be scaled by "weights" w_j so that the sum $\sum_j A_{ij} w_j$ best matches the hit counts in data d_i. This problem is solved taking into account the Poisson nature of both data and simulation sets of each cascade (as described in [4]), resulting in the set of unfolded simulation weights w_i. The first guess is obtained by solving the $\sum_j A_{ij} w_j = d_i$ with a non-negative least squares (NNLS) algorithm, and the solution is then refined for the full likelihood description with a derivative method (BFGS2 of GSL, [8]).

The unfolding procedure is repeated for various values of t_0, and the best value of t_0 is chosen to maximize the likelihood comparing the data with a superposition of cascades weighted with the unfolded weights w_j determined for that t_0. The unfolded pattern of weights corresponding to the best value of t_0 is applied to the energies of cascades along the track, and the event is re-simulated.

The procedure described above is optionally repeated one more time (second pass) starting with small cascades of energies proportional to w_j (but still with a total sum of 10^6 GeV), adding simulation to the pool created during the first pass (i.e., simulation sets from both passes are used for the energy loss unfolding part of the calculation, and for the fit to t_0). The final pattern of cascade energies is re-simulated one more time and the final likelihood value for this iteration is computed.

The entire calculation described in this section is performed for each of the 25 trial sets of each of the 400 iterations of section 2. Fig. 4 demonstrates the convergence behavior of the method for a track event.

4 Estimating uncertainties

Statistical uncertainties can be estimated with an Approximate Bayesian Computation (ABC) method as in [9, 10].

The idea is to substitute the probability of data D given event parameters θ, $p(D|\theta)$, in the Bayes expression for the conditional probability density

$$p(\theta|D) = \frac{p(D|\theta) \cdot p(\theta)}{p(D)},$$

with a probability to obtain data events that are sufficiently similar to the event under investigation. The similarity is defined with a "distance" between the other possible data events $\hat{D}$ and our data event D

$$\rho(\hat{D}, D) \leq \varepsilon,$$

which we substitute with the minus log likelihood expression of [4], comparing the time-binned photo-electron charges between data and simulation.

Since the prior of the track parameters x, y, z, θ, ϕ can be often assumed to be flat in 3D space of coordinates and on a 2D sphere of directions (as neutrinos interact uniformly anywhere inside the detector), the sampling method of choice is a Markov Chain (rather than rejection), where steps are sampled from a proposal distribution and accepted when the "distance" condition is satisfied. For more details of this procedure (including a proof), see [9]. The parameters of the proposal distribution and ε in the "distance" expression are estimated from the best steps of the minimization procedure of sections 2 and 3.

Estimating statistical uncertainties using this method takes approximately the same amount of time as the reconstruction (two days on a specially-configured computer). It is unclear if adding nuisance parameters to this procedure to additionally account for the systematic uncertainties is realistic as the step acceptance rate is lowered with each additional parameter (leading to a "curse of dimensionality").

5 Reconstruction Examples

The method of this report was applied to the 28 high energy events of [11]. Figure 1 compares the reconstructed energy and zenith with the main reconstruction method used in [11]. Most of the points are within the average estimated uncertainties of 10% in energy and 10 degrees in the zenith

angle. The energy of the outlier is overestimated by the reconstruction method of [11], since it did not include the effect of the ice layer tilt (change in depth of a given ice layer at different *x*, *y* across the detector, see [2]) in the PDF used by the reconstruction, whereas the method of this report used our best description of the ice, including the tilt. This particular event was affected more than others because it lay at coordinates just above the dust peak (layer of ice inside the detector volume containing the most dust, at around 2000 m, see [2]), and where the correction due to tilt was significant, affecting whether the event appears to be inside or outside the dust peak ice layer. The uncertainties for this event were estimated in [11] by reconstructing events similar to this one, simulated with the best knowledge of ice. The median of the energy uncertainty range was found to be a good agreement with the energy reconstructed with the method of this report. The outlier in zenith is for a cascade event with a particularly poor reconstructed angular resolution.

Out of the 28 events only one reconstructed as a track, with many reconstructed energy losses along its path (as shown in figure 2, also see figure 3). In the other 6 events that have a muon in addition to the larger cascade the muon part of the event is largely ignored by this reconstruction. We believe this happens when the contribution to the likelihood from the few hits left by the muon is so small that it is largely "washed out" by the fluctuations of the much larger contribution from the cascade part of the event. Finally, figure 4 illustrates how the method converges to the solution, and figure 5 shows a plot of reconstructed uncertainties in direction and energy vs. reconstructed energy.

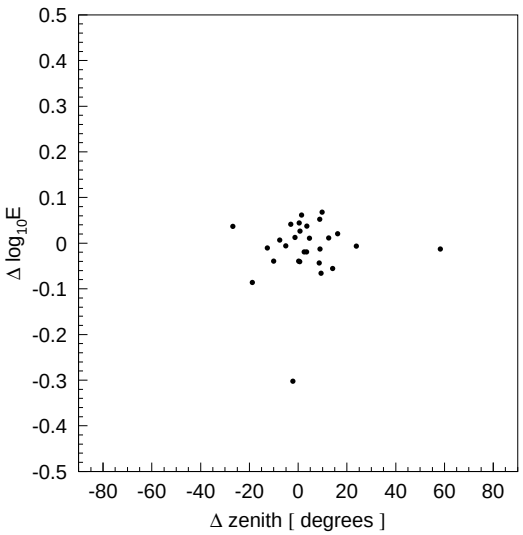


Figure 1: Comparison between the results of the reconstruction method described in this report with the main reconstruction used in [11] for the 28 high energy events of [11].

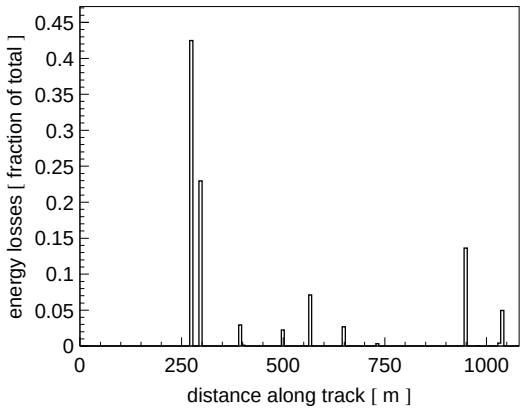


Figure 2: Reconstructed energy losses along the best-fit track of a track-like event shown in figure 3 (one of the 28 high energy events of [11]). The losses are normalized to the total energy lost in the volume of the detector.

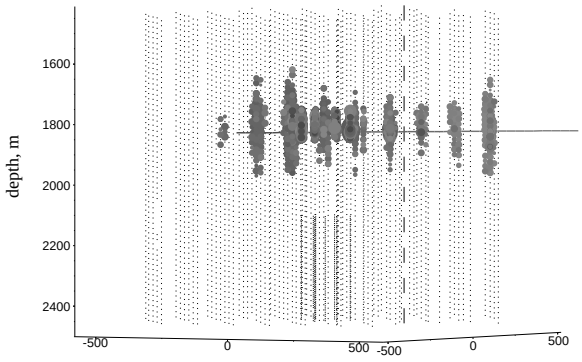


Figure 3: Illustration of a track-like event, one of the 28 high energy events of [11].

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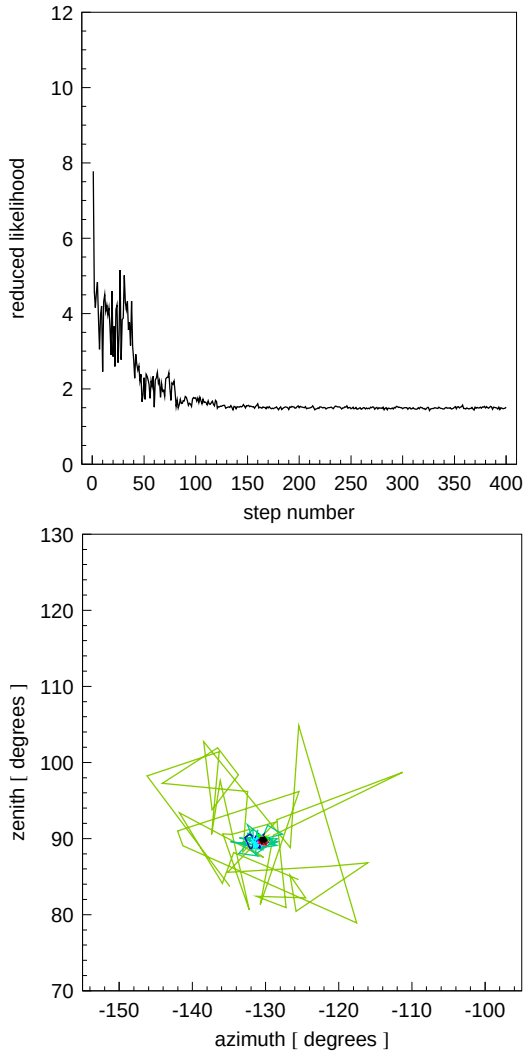


Figure 4: Top: Reduced log likelihood (log likelihood divided by the number of degrees of freedom) after each of the 400 iterations. Some stepping structure evident in the plot is related to the fact that the parameters of the proposal distribution are updated every 40 steps. Bottom: Convergence of the best fit direction: results of successive iterations are connected by line segments for visual clarity. This is a reconstruction of a well-defined track, and results in the method wandering around in a very narrow range of zenith and azimuth. This reconstruction took about 2 days on a computer with 5 GPUs. Most of the calculation time was spent on the GPUs, which were used to run the photon propagation simulation.

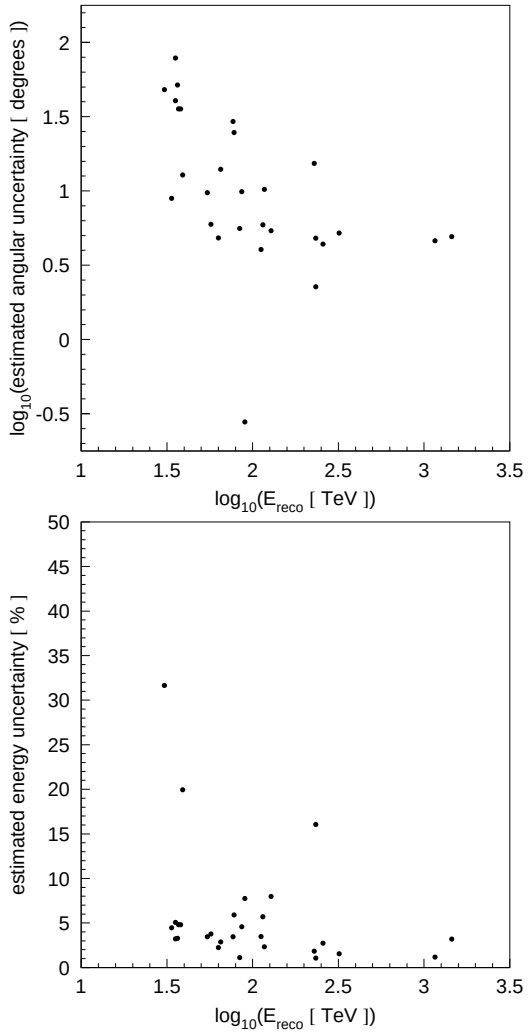


Figure 5: Estimated angular (top) and energy (bottom) statistical uncertainties of the 28 high energy events of [11] as a function of reconstructed energy deposited in the detector volume. The uncertainties shown were calculated as the "spread" of the reconstructed parameters, as explained in section 2.