

**TESTING ALTERNATIVE OSCILLATION SCENARIOS  
WITH ATMOSPHERIC NEUTRINOS USING AMANDA-II  
DATA FROM 2000 TO 2003**

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The AMANDA-II neutrino telescope detects upward-going atmospheric muon neutrinos penetrating the Earth from the Northern Hemisphere via the Cherenkov light of neutrino-induced muons, allowing the reconstruction of the original neutrino direction. Due to the high energy threshold of about 50 GeV, the declination spectrum is minimally affected by mass-induced neutrino oscillations; however, alternative oscillation models predicting effects at high energy can be tested and constrained. Of particular interest are models that allow one to test Lorentz invariance and the equivalence principle. Using the AMANDA-II data from the years 2000 to 2003, a sample of 3401 candidate neutrino-induced events was selected. No indication for alternative oscillation effects was found. For maximal mixing angles, an upper limit is set on both the Lorentz violation parameter  $\delta c/c$  and the equivalence principle violation parameter  $2|\phi|\delta\gamma$  of  $5.3 \times 10^{-27}$  at the 90% confidence level.

**1. Introduction and detector description**

- 2 Cosmic ray particles entering the Earth's atmosphere generate a steady
- 3 flux of secondary particles, including muons and neutrinos. High energy
- 4 muons pass through the atmosphere and can penetrate several kilometers

of ice and rock, while atmospheric neutrinos of energies only above roughly 40 TeV start to be absorbed in the Earth. Lower energy muon neutrinos penetrating the diameter of the Earth can oscillate into tau neutrinos. However, the oscillation maxima at 30 GeV<sup>1</sup> and below are beneath the AMANDA-II threshold. Departures from conventional mass-induced oscillations could emerge at higher neutrino energies due to relativity-violating effects (see below). Such mechanisms would distort the expected angular distribution and energy spectrum of atmospheric neutrinos and could be detectable by AMANDA-II.

The AMANDA-II neutrino telescope is embedded 1500 – 2000 m deep in the transparent and inert ice of the Antarctic ice sheet, close to the geographic South Pole. AMANDA-II consists of 677 optical modules (OMs) on 19 vertical strings, which are arranged in three approximately concentric circles of 60 m, 120 m and 200 m diameter. Muons produced in  $\nu_\mu$ -nucleon interactions can be directionally reconstructed by observing the Cherenkov radiation that propagates through the ice to the array of photosensors. To ensure that the observed muon is due to a neutrino interaction, the Earth is used as a filter against atmospheric muons, and only tracks from the Northern Hemisphere (declination  $\delta > 0^\circ$ ) are selected.

## 2. Phenomenology of standard and alternative neutrino oscillations

It is commonly accepted that standard (mass-induced)  $\nu_\mu \rightarrow \nu_\tau$  oscillations<sup>a</sup> are responsible for the measured deficit of atmospheric muon neutrinos<sup>1</sup>. Atmospheric neutrino data can also be used to test non-standard oscillation mechanisms that lead to observable differences at higher neutrino energies. Various new physics scenarios can result in neutrino flavor mixing. Two of these scenarios, which can be described in a mathematically analogous way, have been tested in this analysis. The underlying theories assume small deviations from the principles of the theory of relativity and lead to measurable neutrino oscillations:

- In theories predicting violation of Lorentz invariance (VLI), a set of additional neutrino eigenstates with different maximal attainable velocities (MAV)  $c_n/c$  is introduced, violating special relativity<sup>2</sup>.

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<sup>a</sup>In the regime of atmospheric neutrino oscillations, it suffices to consider a two-flavor system of eigenstates ( $\nu_\mu, \nu_\tau$ ).

- In theories predicting violation of the weak equivalence principle (VEP), gravitational neutrino eigenstates are introduced which couple with distinct strengths  $\gamma_n$  to a gravitational potential  $\phi$ , conflicting with the universal coupling assumed in general relativity<sup>3,4</sup>.

The main difference between these oscillation scenarios and standard oscillations is the linear energy dependence of the oscillation frequency, shifting observable oscillation effects into the energy range of AMANDA-II. For the sake of simplicity, we will focus on the VLI scenario. As both theories are mathematically equivalent, the results can be transferred to the VEP case by simply exchanging the relativity-violating oscillation parameters  $\delta c/c \rightarrow 2|\phi|\delta\gamma$  and mixing angles  $\Theta_c \rightarrow \Theta_\gamma$ .

Combining standard and VLI oscillations, one obtains three systems of neutrino eigenstates (flavor, mass, and MAV eigenstates), resulting in a total of 5 oscillation parameters: the mass-squared difference  $\Delta m^2$ , two mixing angles  $\Theta_m$  and  $\Theta_c$ , the VLI parameter  $\delta c/c$ , and a complex phase  $\eta$ . Fixing  $\Delta m^2 = 2.3 \times 10^{-3} \text{ eV}^2$  and  $\Theta_m = 45^\circ$ , the survival probability may then be written as:

$$P(\nu_\mu \rightarrow \nu_\mu) = 1 - \sin^2 2\Theta \sin^2(\Omega L) \quad (1)$$

$$2\Theta = \arctan(s/t) \quad \Omega = \sqrt{s^2 + t^2} \quad (2)$$

$$\begin{aligned} s &= 2.92 \times 10^{-3} |1/E_\nu + 8.70 \times 10^{20} \delta c/c \sin 2\Theta_c E_\nu e^{i\eta}|, \\ t &= 2.54 \times 10^{18} \delta c/c \cos 2\Theta_c E_\nu. \end{aligned} \quad (3)$$

Here the muon neutrino path length  $L$  is expressed in km and the neutrino energy  $E_\nu$  in GeV. For the given set of parameters, one can observe a significant effect within the analyzed energy range (100 GeV – 10 TeV) and declination range ( $\delta \geq 20^\circ$ ), for certain values of  $\Theta_c$  and  $\delta c/c$ .

The VLI effects can also be viewed in terms of the Standard Model Extension, an effective quantum field theory which adds all coordinate-independent renormalizable Lorentz-violating operators to the Standard Model<sup>5,6</sup>. In particular, the above oscillations correspond to non-zero and differing eigenvalues of  $c_L$ , the dimensionless coefficient of the Lorentz-violating Lagrangian term  $\frac{1}{2}i(c_L)_{\mu\nu ab}\bar{L}_a\gamma^\mu\overleftrightarrow{D}^\nu L_b$ <sup>7</sup>. Additionally, in this scenario only rotationally invariant (time) components of  $c_L$  are non-zero (so-called “fried chicken” models), and we consider only a two-flavor system. With these restrictions,  $\delta c/c$  in eq. 3 is equivalent to the difference in eigenvalues ( $c_a - c_b$ ) of the  $2 \times 2$  matrix  $c_L^{TT}$ .

### 76 3. Data selection and analysis method

77 The data analyzed in this analysis are selected from  $7.9 \times 10^9$  events recorded  
 78 from 2000 to 2003, representing a total livetime of 807.2 days. Quality se-  
 79 lection criteria based on various track reconstruction quantities are used  
 80 to reduce contamination of the sample by mis-reconstructed atmospheric  
 81 muons to a level of approximately 4% (see ref. 8 for more details). The re-  
 82 sulting number of selected neutrino candidate events is 3401. Reconstructed  
 83 declination and the number of OMs triggered in an event ( $N_{\text{ch}}$ , an energy  
 84 estimator) are used as observables to search for any deviations in the atmo-  
 85 spheric neutrino spectrum that are dependent on flight length or neutrino  
 86 energy. A full simulation chain, including neutrino absorption in the Earth,  
 87 neutral current regeneration, muon propagation, and detector response is  
 88 used to simulate the response of AMANDA-II to atmospheric neutrinos<sup>9,10</sup>.  
 89 The expected atmospheric muon neutrino flux before oscillations is taken  
 90 from Lipari<sup>11</sup>.

91 The analysis method uses a  $\chi^2$ -test to compare the declination and  $N_{\text{ch}}$   
 92 distributions of data with Monte Carlo simulations including VLI oscillation  
 93 effects. The systematic uncertainties affecting the Monte Carlo prediction  
 94 are integrated into the  $\chi^2$  expression: uncertainties in the normalization  
 95 due to detector response and theoretical models of atmospheric neutrino  
 96 flux (30%); uncertainty due to the relative production rate between kaons  
 97 and pions (6%); and uncertainty in the sensitivity of the OMs (11.5%).  
 98 The optimal binning of the  $\chi^2$  expression is determined using toy Monte  
 99 Carlo studies, and the exclusion regions for alternative oscillation effects  
 100 are obtained by scanning through the oscillation parameter space.

### 101 4. Results and Outlook

102 The analysis of the final atmospheric neutrino sample finds no evidence for  
 103 alternative oscillations, and a preliminary upper limit on the VLI parameter  
 104  $\delta c/c$  is set of  $5.3 \times 10^{-27}$  at the 90% confidence level, for nearly maximal  
 105 mixing angles  $\Theta_c \approx \pm\pi/4$ . The dependence on the unconstrained phase  $\eta$   
 106 is found to be small (see figure 1); the most conservative limit is obtained  
 107 for  $\cos\eta = 0$ . The limit can also be interpreted in the context of VEP  
 108 theories, leading to an upper limit of  $2|\phi|\delta\gamma \leq 5.3 \times 10^{-27}$ . This result is  
 109 competitive with the limits obtained using data from Super-Kamiokande<sup>12</sup>  
 110 and MACRO<sup>13</sup>. However, AMANDA is not sensitive to small mixing angles  
 111 due to the systematic errors and its higher energy threshold.

112 A likelihood analysis of the 2000-2006 AMANDA-II data sample is

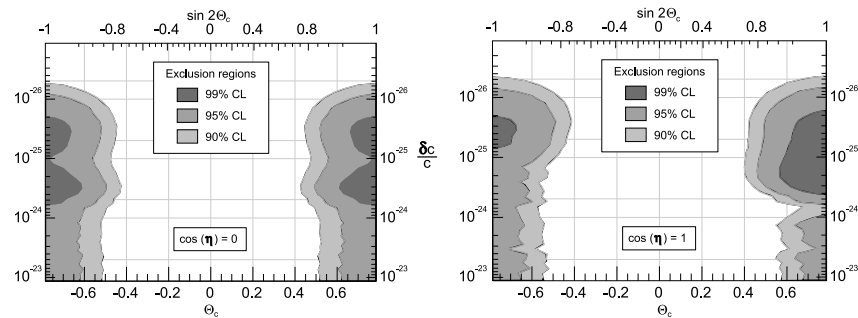


Figure 1. Shown are preliminary exclusion regions for VLI (VEP) oscillation effects, left for  $\cos \eta = 0$ , right for  $\cos \eta = 1$ .

113 in progress, with improved systematic error estimation and increased  
 114 sensitivity<sup>14</sup>. This analysis will also extend the technique to search for  
 115 evidence of quantum decoherence resulting from interaction of neutrinos  
 116 with the background space-time foam<sup>15</sup>. The next-generation IceCube de-  
 117 tector, when completed in 2010, will be able to extend the sensitivity to  
 118 VLI effects by about one order of magnitude<sup>16</sup>.

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